

# Design of a H<sub>2</sub> PSA for cogeneration of ultrapure hydrogen and power at an advanced integrated gasification combined cycle with pre-combustion capture

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**Abstract** A novel hydrogen pressure swing adsorption system has been studied that is applied to an advanced integrated gasification combined cycle plant for cogenerating power and ultrapure hydrogen (99.99+ mol%) with CO<sub>2</sub> capture. In designing the H<sub>2</sub> PSA, it is essential to increase the recovery of ultrapure hydrogen product to its maximum since the power consumption for compressing the H<sub>2</sub> PSA tail gas up to the gas turbine operating pressure should be minimised to save the total auxiliary power consumption of the advanced IGCC plant. In this study, it is sought to increase the H<sub>2</sub> recovery by increasing the complexity of the PSA step configuration that enables a PSA cycle to have a lower feed flow to one column for adsorption and more pressure equalisation steps. As a result the H<sub>2</sub> recovery reaches a maximum around 93 % with a Polybed H<sub>2</sub> PSA system having twelve columns and the step configuration contains simultaneous adsorption at three columns and four-stage pressure equalisation.

**Keywords** IGCC · Pressure swing adsorption · Hydrogen purification · Cogeneration

## Nomenclature

$A_c$	Internal column surface area, m <sup>2</sup>
$A_p$	Pellet surface area, m <sup>2</sup>
$b_i^j$	Adsorption equilibrium constant of site j for comp. i, bar <sup>-1</sup>
$b_{i,0}^j$	Pre-exponential adsorption equilibrium constant coefficient of site j for comp. i, bar <sup>-1</sup>
$c_i$	Gas concentration of component i, mol m <sup>-3</sup>

$c_i^m$	Gas concentration of component i in the macropore, mol m <sup>-3</sup>
$c_T$	Total gas concentration, mol m <sup>-3</sup>
$c_{P,s}$	Specific heat capacity at constant pressure of the adsorbent, J kg <sup>-1</sup> K <sup>-1</sup>
$D^L$	Axial mass dispersion coefficient, m <sup>2</sup> s <sup>-1</sup>
$D_c$	Column diameter, m
$D_m$	Molecular diffusivity, m <sup>2</sup> s <sup>-1</sup>
$D_{p,i}$	Macropore diffusivity of component i, m <sup>2</sup> s <sup>-1</sup>
$d_p$	Pellet averaged diameter, m
$h_w$	Heat transfer coefficient at the column wall, W m <sup>-2</sup> K <sup>-1</sup>
$H_f$	Enthalpy in the fluid phase per unit volume, J m <sup>-3</sup>
$\tilde{H}_i$	Partial molar enthalpy in the fluid phase of component i, J mol <sup>-1</sup>
$\Delta\tilde{H}_i^j$	Heat of adsorption of site j for component i, J mol <sup>-1</sup>
$J_i$	Diffusive flux of component i, mol m <sup>-2</sup> s <sup>-1</sup>
$J_T$	Thermal diffusive flux, W m <sup>-2</sup>
$k_g$	Gas conductivity, W m <sup>-1</sup> K <sup>-1</sup>
$k_i^p \cdot A_p / V_p$	LDF mass transfer coefficient of component i in the pellet, s <sup>-1</sup>
$k_i^{cr} \cdot 3 / r_c$	LDF mass transfer coefficient of component i in the crystal, s <sup>-1</sup>
$L_c$	Column length, m
$M_{ads}$	Adsorbent mass, kg
$P$	Pressure, bar
$Pr$	Prandtl number, [-]
$\bar{q}_i$	Average adsorbed concentration of component i in the crystal, mol kg <sup>-1</sup>
$q_i^*$	Adsorbed concentration of component i at equilibrium, mol kg <sup>-1</sup>
$q_{i,s}^j$	Saturation capacity of site j for comp. i, mol kg <sup>-1</sup>

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$\bar{Q}_i$	Average adsorbed concentration of component $i$ in the pellet, $\text{mol m}^{-3}$
$Q_{\text{feed}}$	Feed flow rate, $\text{mol s}^{-1}$
$R$	Ideal gas constant $\text{J mol}^{-1} \text{K}^{-1}$
$Re$	Reynolds number, [-]
$r_c$	Crystal radius, m
$r_p$	Pellet radius, m
$Sc$	Schmidt number, [-]
$t$	Time, s
$t_{\text{cycle}}$	Cycle time, s
$T$	Temperature, K
$T_f$	Fluid temperature, K
$T_w$	Column wall temperature, K
$u$	Velocity, $\text{m s}^{-1}$
$U_f$	Internal energy in the fluid phase per unit volume, $\text{J m}^{-3}$
$U_p$	Internal energy in the pellet per unit volume, $\text{J m}^{-3}$
$U_{p,f}$	Internal energy in the macropore per unit volume, $\text{J m}^{-3}$
$U_{p,s}$	Internal energy in the solid phase per unit volume, $\text{J m}^{-3}$
$v$	Interstitial flow velocity, $\text{m s}^{-1}$
$V_c$	Column volume, $\text{m}^3$
$V_p$	Pellet volume, $\text{m}^3$
$x_i, y_i$	Molar fraction of component $i$ , [-]
$z$	Spatial dimension, m

### Greek letters

$\varepsilon$	External bed void fraction, [-]
$\varepsilon_p$	Pellet void fraction, [-]
$\lambda^L$	Axial thermal dispersion coefficient, $\text{W m}^{-1} \text{K}^{-1}$
$\mu$	Viscosity, $\text{bar s}$
$\rho_f$	Fluid density, $\text{kg m}^{-3}$
$\rho_p$	Pellet density, $\text{kg m}^{-3}$

## 1 Introduction

Eight refineries in the UK are currently emitting 14.9  $\text{MtCO}_2$  which accounts for around 3 % of total UK  $\text{CO}_2$  emission in 2009 (DECC 2009). The INEOS refining plant in Grangemouth, for example, emits around 2.2  $\text{MtCO}_2$  per annum, which is equivalent to 4 % of total  $\text{CO}_2$  emissions in Scotland (SEPA 2008). The Committee on Climate Change (CCC) estimated that there will be a chance to curtail around 3.5  $\text{MtCO}_2$  out of 14.9  $\text{MtCO}_2$  from refineries by 2030 by improving their energy efficiency. The CCC also foresaw that beyond this target of abatement, a further reduction would be possible by deploying carbon capture units on  $\text{H}_2$  plants and replacing combustion fuels with carbon-neutral biomass (Committee on Climate Change 2011).

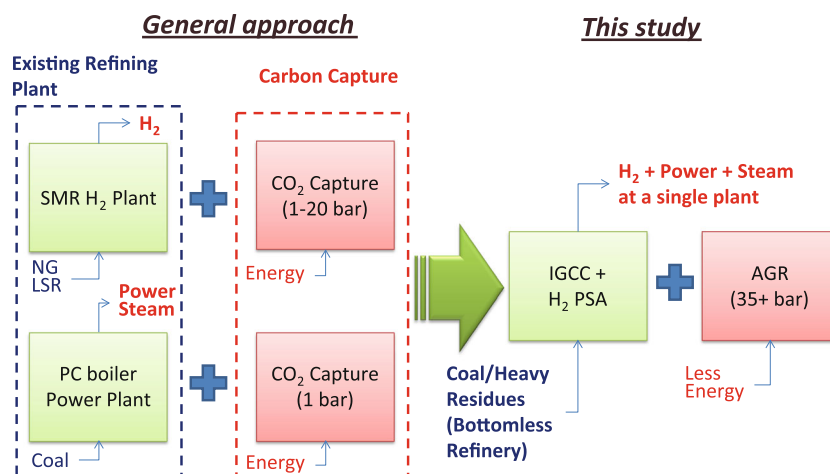
It is well known that most refining complexes face a significant deficiency of their existing hydrogen production capacity. Hydrogen is needed for operating their hydro-treating desulphurisation process that removes mainly sulphur and other impurities from raw petroleum products and hydrocracking units for upgrading low-grade heavy residues to more valuable diesel and lube base oil. The need for  $\text{H}_2$  is bound to increase due to the trends of (1) more stringent sulphur and nitrogen specification in fuel oils, (2) increasing crack spread, and (3) the rapid change of crude oil properties from ‘light and sweet’ to ‘heavy and sour’. Due to the requirement of very high operational severity in both units for deep desulphurisation and improved product quality, ultrapure hydrogen with a purity of 99.99+ mol% should be utilised for the hydroprocessing. Accordingly, most refineries are forced to increase rapidly their hydrogen production capacities to cope with the increased  $\text{H}_2$  demand but it is doubtful that given the upcoming carbon emission regulation conventional steam methane reforming (SMR)  $\text{H}_2$  processes would be still the best option to meet this demand.

Most refineries have their own power plant to provide various units with the utilities such as steam and electricity. In particular, when integrated with a carbon capture unit, integrated gasification combined cycle (IGCC) power plants would have significantly lower energy penalty than coal-fired power plants since a carbon capture unit can be applied to a gas stream having higher  $\text{CO}_2$  partial pressure in IGCC power plants. As a result, it has been reported that IGCC power plants integrated with pre-combustion capture would have notably higher net power efficiency than coal fired power plants (DOE 2007).

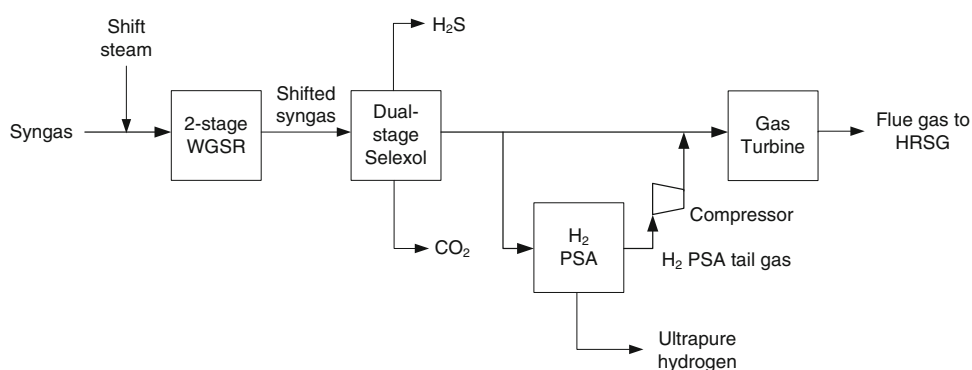
It should also be noted that IGCC power plants run gas turbines using  $\text{H}_2$ -rich fuel gas (88–91 mol%  $\text{H}_2$  purity) in  $\text{CO}_2$  capture cases instead of mixtures of  $\text{CO}$  and  $\text{H}_2$  in non-capture cases and it is easy to produce ultrapure hydrogen product by purifying the  $\text{H}_2$ -rich fuel gas. This means that by replacing both the existing SMR  $\text{H}_2$  plant and the coal-fired power plants with an advanced IGCC plant it would be possible to provide refining complexes with ultrapure  $\text{H}_2$  and power simultaneously where  $\text{CO}_2$  can be inherently captured as depicted in Fig. 1.

In producing ultrapure hydrogen (99.99+ mol%) from such a gas mixture as composed of  $\text{H}_2$ ,  $\text{CO}_2$ ,  $\text{CO}$ ,  $\text{N}_2$  and  $\text{Ar}$ , it is well-known that a pressure swing adsorption (PSA) is the only economically feasible, commercialised separation process. The multi-column PSA process, known as UOP Polybed, has been widely applied to SMR  $\text{H}_2$  plants to produce ultrapure  $\text{H}_2$  from shifted syngas. However, the conventional  $\text{H}_2$  PSA has been designed and optimised against a feed stream of around 71 %  $\text{H}_2$ , 19 %  $\text{CO}_2$ , 4 %  $\text{CO}$  and 5 %  $\text{CH}_4$  at 20 bar found in a SMR  $\text{H}_2$  process. This composition and the pressure of the raw  $\text{H}_2$  feed in a

**Fig. 1** A conceptual diagram to compare general approach to capture CO<sub>2</sub> from a SMR H<sub>2</sub> plant and a coal-fired power plant separately to an advanced IGCC process for cogenerating power and ultrapure hydrogen with carbon capture (this study)



**Fig. 2** Block flow diagram of an advanced IGCC process for cogenerating power and ultrapure hydrogen



SMR-based H<sub>2</sub> plant is quite different from the raw H<sub>2</sub> fuel gas in IGCC power plants with carbon capture (88.75 % H<sub>2</sub>, 2.12 % CO<sub>2</sub>, 2.66 % CO, 5.44 % N<sub>2</sub>, 1.03 % Ar at 34 bar). Therefore, there is a need to revisit the design of the H<sub>2</sub> PSA process to estimate the H<sub>2</sub> recovery and productivity obtained at the operating conditions to meet the H<sub>2</sub> product purity as high as 99.99+ mol%.

## 2 Design basis of a H<sub>2</sub> PSA integrated with an IGCC power plant

This study is aimed at the design of a H<sub>2</sub> PSA system that is applicable to an advanced IGCC plant for producing both ultrapure H<sub>2</sub> and power. The advanced IGCC plant is a modification of a conventional IGCC power plant with carbon capture to include a new H<sub>2</sub> PSA unit and its block flow diagram is illustrated in Fig. 2.

The process design of the conventional IGCC power plants with carbon capture is based on an exemplary IGCC power plant using a Shell gasifier (DOE 2007; Kapetaki et al. 2013). The syngas stream from the shift reactors is fed to an acid gas removal unit (AGR), such as a dual-stage Selexol unit, to remove CO<sub>2</sub> as well as H<sub>2</sub>S from the

syngas. In the conventional IGCC process, the treated syngas leaving the AGR becomes saturated with water in a fuel gas saturation column and then is fed to the combustion chamber of a gas turbine. But in this study the treated syngas is split into two streams: one stream flows directly to a gas turbine for power generation and the other is sent to a H<sub>2</sub> PSA for ultrapure H<sub>2</sub> production. The H<sub>2</sub> PSA tail gas obtained as by-product needs to be compressed up to the operating pressure of the gas turbine and sent to the combustion chamber with the H<sub>2</sub>-rich fuel gas.

Various H<sub>2</sub> PSA designs have been studied so far in order to estimate their performance when they are applied to conventional SMR H<sub>2</sub> plants (Ribeiro et al. 2008, 2009; Lopes et al. 2011). Even though the H<sub>2</sub> recovery that is expected of a commercial Polybed H<sub>2</sub> PSA in a SMR H<sub>2</sub> plant is as high as 89 %, they could obtain 52 to 80 % H<sub>2</sub> recovery at around 99.99 mol% H<sub>2</sub> purity. This is because the H<sub>2</sub> PSA systems in their design were configured with maximum four columns while commercial Polybed H<sub>2</sub> PSA systems in most cases contain seven to sixteen adsorption columns to enable enhanced hydrogen recovery. In this study, H<sub>2</sub> PSA systems having up to twelve columns have been simulated to see the effect of different PSA step configurations that are subject to the chosen number of

columns on the  $H_2$  recovery using an in-house cyclic adsorption process simulator (Friedrich et al. 2013).

Given the composition and the pressure of raw  $H_2$  feeds that previous study dealt with (Ahn et al. 2001), it was concluded that  $H_2$  PSA designs that were configured with adsorption columns having two adsorbent layers would exhibit a better performance than those having adsorption columns packed with a single adsorbent. This is because it is unlikely to find a versatile adsorbent that has better working capacities than others for all impurities being contained in a raw  $H_2$  feed. Therefore, a layered bed is usually configured such that an activated carbon layer near the feed end plays a role in adsorbing mainly  $CO_2$  and  $CH_4$  while a zeolite layer on top of the activated carbon layer removes  $CO$  and  $N_2$ . The length ratio of the carbon to zeolite layers is regarded as one of the key parameters that need to be optimised (Ahn et al. 2001, 2012; Ribeiro et al. 2008; Yang and Lee 1998; Park et al. 1998). Given the composition of the new raw  $H_2$  feed that has relatively small  $CO_2$  and no  $CH_4$ , however, it is plausible that an adsorption column packed with zeolite 5A performs better than those with a layered bed of activated carbon and zeolite 5A.

The production of the  $H_2$  PSA tail gas should be minimised in order to reduce the power consumption relating to its compression before feeding it to the gas turbine. In this study the aim is to maximise  $H_2$  recovery by adding more columns to the  $H_2$  PSA process to enable more complicated step configurations for minimising the  $H_2$  loss and consumption. To know the maximum hydrogen recovery that a  $H_2$  PSA could achieve is essential in determining the mass balance around the  $H_2$  PSA, i.e. the flowrate and the composition of both ultrapure hydrogen product and PSA tail gas. Once the mass balance is constructed at the condition of achieving the maximum  $H_2$  recovery, it is possible to estimate the auxiliary power consumption in compressing the  $H_2$  PSA tail gas and the power generation in the gas and steam turbines accurately.

### 3 $H_2$ PSA simulation

The dynamic behaviour of a  $H_2$  PSA is described by a mathematical model which couples mass, momentum and energy balances over a packed bed with the appropriate boundary conditions for each step of the cycle (Friedrich et al. 2013).

Since the flow is assumed to be a dispersed plug flow the component and overall material balances along the column are given by:

$$\frac{\partial c_i}{\partial t} + \frac{(1-\varepsilon)}{\varepsilon} \cdot \frac{\partial \bar{Q}_i}{\partial t} + \frac{\partial(c_i \cdot v)}{\partial z} + \frac{\partial J_i}{\partial z} = 0 \quad (1)$$

$$\bar{Q}_i = \varepsilon_p c_i^m + \rho_p \bar{q}_i \quad (2)$$

$$J_i = -D^L c_T \frac{\partial x_i}{\partial z} \quad (3)$$

$$\frac{\partial c_T}{\partial t} + \frac{(1-\varepsilon)}{\varepsilon} \cdot \sum_i \frac{\partial \bar{Q}_i}{\partial t} + \frac{\partial(c_T \cdot v)}{\partial z} = 0 \quad (4)$$

Since the column undergoes significant temperature excursions over a cycle caused by the heat of adsorption, constitutive energy balances are coupled with the mass balance:

$$\varepsilon \frac{\partial U_f}{\partial t} + (1-\varepsilon) \frac{\partial U_P}{\partial t} + \varepsilon \frac{\partial(H_f \cdot v)}{\partial z} + \frac{\partial J_T}{\partial z} + \sum_{i=1}^{N_c} \frac{\partial(J_i \bar{H}_i)}{\partial z} + h_w \frac{A_c}{V_c} (T_f - T_w) = 0 \quad (5)$$

$$\frac{dU_P}{dt} = \varepsilon_p \frac{dU_{P,f}}{dt} + (1-\varepsilon_p) \frac{dU_{P,s}}{dt} \quad (6)$$

$$J_T = -\lambda^L \varepsilon \frac{\partial T_f}{\partial z} \quad (7)$$

In Eq. (5),  $T_w$  is assumed to be equal to ambient temperature since a heat balance around the wall is not taken into account.

In this work the adsorption rate is represented by Linear Driving Force (LDF) model for both macropores and micropores.

$$\varepsilon_p \frac{dc_i^m}{dt} + \rho_p \frac{d\bar{q}_i}{dt} = k_i^p \frac{A_p}{V_p} (c_i - c_i^m) \quad (8)$$

$$k_i^p \frac{A_p}{V_p} = \frac{15 \cdot \varepsilon_p \cdot D_{p,i}}{r_p^2} \quad (9)$$

$$\frac{d\bar{q}_i}{dt} = k_i^{cr} \frac{3}{r_c} (q_i^* - \bar{q}_i) \quad (10)$$

The axial mass dispersion coefficient  $D^L$  and the axial thermal dispersion coefficient  $\lambda^L$  are estimated using the correlations by Wakao and Funazkri (1978):

$$\frac{\varepsilon \cdot D^L}{D_m} = 20 + 0.5 \cdot Sc \cdot Re \quad (11)$$

$$\frac{\lambda^L}{k_g} = 7 + 0.5 \cdot Pr \cdot Re \quad (12)$$

The pressure drop along the column is evaluated using the Ergun equation (Ergun 1952):

$$-\frac{\partial P}{\partial z} = \frac{150\mu(1-\varepsilon)^2}{d_p^2 \varepsilon^2} v + \frac{1.75\rho_f(1-\varepsilon)}{d_p \varepsilon} v|v| \quad (13)$$

The boundary conditions for the gas phase concentrations and the enthalpies are given by the Danckwerts boundary conditions. With the conventions that the positive flow direction is from 0 (feed end) to  $L$  (product end) these can be written in a general form as:

**Table 1** Isotherm parameters of dual-site Langmuir model for zeolite 5A

Gas	$q_{i,s}^1$ (mol/kg)	$q_{i,s}^2$ (mol/kg)	$b_{i,0}^1$ (bar <sup>-1</sup> )	$b_{i,0}^2$ (bar <sup>-1</sup> )	$(-\Delta H_i^1)$ (J/mol)	$(-\Delta H_i^2)$ (J/mol)
CO <sub>2</sub>	0.7077	3.711	$1.077 \times 10^{-7}$	$1.233 \times 10^{-4}$	38,312	29,808
H <sub>2</sub>	0.7077	3.711	$4.227 \times 10^{-7}$	$1.333 \times 10^{-4}$	19,674	9,282
CO	0.7077	3.711	$2.431 \times 10^{-8}$	$2.321 \times 10^{-5}$	47,736	20,994
N <sub>2</sub>	0.7077	3.711	$2.141 \times 10^{-6}$	$8.987 \times 10^{-5}$	31,338	14,956
Ar	0.7077	3.711	$1.399 \times 10^{-9}$	$4.901 \times 10^{-4}$	50,239	11,171

$$J_T|_{z=0} = \frac{v + |v|}{2} (H_{f,0-} - H_{f,0}) \quad (14)$$

$$J_T|_{z=L_c} = \frac{v - |v|}{2} (H_{f,L_c+} - H_{f,L_c}) \quad (15)$$

$$J_i|_{z=0} = \frac{v + |v|}{2} (c_{i,0-} - c_{i,0}) \quad (16)$$

$$J_i|_{z=L_c} = \frac{v - |v|}{2} (c_{i,L_c+} - c_{i,L_c}) \quad (17)$$

Adsorption equilibrium of pure hydrogen, carbon dioxide, carbon monoxide, nitrogen and argon on zeolite 5A are reported in the literature in the range of the pressure up to 7.5 bar (Lopes et al. 2009). The adsorption equilibria are predicted by the following extended dual-site Langmuir model:

$$q_i^* = \frac{q_{i,s}^1 b_i^1 P x_i}{1 + \sum_{j=1}^{N_c} b_j^1 P x_j} + \frac{q_{i,s}^2 b_i^2 P x_i}{1 + \sum_{j=1}^{N_c} b_j^2 P x_j} \quad (18)$$

with  $b_i^l = b_{i,0}^l \exp\left(\frac{-\Delta \bar{H}_i^l}{RT}\right)$ .

Experimental data (Lopes et al. 2009) are fitted using Origin 8.5 (OriginLab 2010). The isotherm parameters of dual-site Langmuir model are given in Table 1.

Cycle performances are evaluated according to the common parameters of H<sub>2</sub> purity, H<sub>2</sub> recovery and H<sub>2</sub> productivity defined as follows:

$$H_2 \text{ Purity} = \frac{\int_0^{t_{AD}} C_{H_2} u|_{z=L} dt}{\sum_i \int_0^{t_{AD}} C_i u|_{z=L} dt} \quad (19)$$

$$H_2 \text{ Recovery} = \frac{\int_0^{t_{AD}} C_{H_2} u|_{z=L} dt - \int_0^{t_{PR}} C_{H_2} u|_{z=L} dt}{\int_0^{t_{AD}} C_{H_2} u|_{z=0} dt} \quad (20)$$

$$H_2 \text{ Productivity} = \frac{(\int_0^{t_{AD}} C_{H_2} u|_{z=L} dt - \int_0^{t_{PR}} C_{H_2} u|_{z=L} dt) A_c}{t_{cycle} M_{ads}} \quad (21)$$

The aim is to design a H<sub>2</sub> PSA process having a capacity of 110 H<sub>2</sub> MMSCFD that is approximately equivalent to 1,609 H<sub>2</sub> mol/s. Given the H<sub>2</sub> mol fraction in the raw H<sub>2</sub> feed, the required flowrate of a raw H<sub>2</sub> feed flowing to the H<sub>2</sub> PSA would be around 2,015 mol/s assuming 90 % H<sub>2</sub> recovery. According to the design of the IGCC power plant

with carbon capture using a Shell dry coal-fed gasifier (DOE Case 6, 2007), the advanced IGCC plant for cogeneration of power and ultrapure hydrogen would be configured such that around 40 % of the raw H<sub>2</sub> gas is directed to the H<sub>2</sub> PSA while the remaining 60 % flows to a syngas humidifier and subsequently a combustion chamber in the gas turbine just as in the conventional IGCC power plant.

Planning as a future work an experimental campaign to validate the simulation results subsequent to this study, the dimension of adsorption columns in this study was determined to be the same as those of a lab-scale six-column PSA rig as shown in Table 2. Given the column size and dimension, the feed flowrate is set at 0.002 mol/s with a scaling factor of 10<sup>-6</sup>. The figures of other parameters used in the simulation are also presented in Table 2. In all the simulations, the set of the partial and ordinary differential equations and the algebraic equations were solved using the in-house CySim simulator. The discretization method for the spatial domain in the column was central finite difference method (CFDM) with 20 grid points along the column. The system of differential algebraic equations was solved with the DAE solver SUNDIALS (Friedrich et al. 2013).

## 4 Simulation results

Five different H<sub>2</sub> PSA systems have been investigated to see the change of H<sub>2</sub> recovery and productivity with different levels of complexity of the step configuration that is subject to the number of columns. The H<sub>2</sub> recovery and productivity obtained at different configurations are compared under the operating condition to meet the specification of the H<sub>2</sub> purity (99.99 mol%) at each configuration. First of all, a four-column H<sub>2</sub> PSA system was simulated and the targeted H<sub>2</sub> purity was obtained at a cycle time of 800 s. Since all the simulations were carried out at constant feed flowrate of 0.002 mol/s, the total cycle time became longer as more columns that are identical in size and dimension were added to configure six-, nine- and twelve-column H<sub>2</sub> PSA systems. This is because either more than one column can share the total feed gas for adsorption at

**Table 2** List of column parameters, particle parameters, and operating conditions of H<sub>2</sub> PSA simulations

Column parameters	
Column length, $L_c$ [m]	0.5
Column internal diameter, $D_c$ [m]	0.025
External bed void fraction, $\varepsilon$ [-]	0.391
Axial mass dispersion coefficient, $D^L$ [m <sup>2</sup> /s]	$1.165 \times 10^{-4}$
Axial thermal dispersion coefficient, $\lambda^L$ [W/m K]	1.279
Wall heat transfer coefficient, $h_w$ [W/m <sup>2</sup> K]	95
Adsorbent parameters	
Pellet density, $\rho_p$ [kg/m <sup>3</sup> ]	1,126
Pellet void fraction, $\varepsilon_p$ [-]	0.503
Adsorbent specific heat capacity, $c_{p,s}$ [J/kg K]	920
Pellet averaged diameter, $d_p$ [mm]	1.70
Macropore LDF coefficient, $k_p^p \times A_p/V_p$ H <sub>2</sub> /CO <sub>2</sub> /CO/N <sub>2</sub> /Ar [s <sup>-1</sup> ]	9.222/6.073/7.518/7.897/7.284
Micropore LDF coefficient, $k_i^{cr} \times 3/r_c$ H <sub>2</sub> /CO <sub>2</sub> /CO/N <sub>2</sub> /Ar [s <sup>-1</sup> ]	0.7467/0.0017/0.0332/0.1697/0.1800 (Lopes et al. 2009)
Operating conditions	
$P_{ads}$ [bar]	34
$P_{des}$ [bar]	1
$T_{feed}$ [K]	303
$Q_{feed}$ [mol/s]	0.002
Feed composition, $y_{H_2}/y_{CO_2}/y_{CO}/y_{N_2}/y_{Ar}$ [molar]	0.8875/0.0212/0.0266/0.0544/0.0103

the same time or more steps need to be included in one cycle. To evaluate whether or not a simulation reaches its cyclic steady state (CSS), the H<sub>2</sub> purity and recovery at a cycle were compared with those at the previous cycle. It was assumed that a cyclic steady state would be reached if the differences of the H<sub>2</sub> purity and recovery between the new and previous cycles were both less than  $10^{-6}$ .

#### 4.1 Four-column H<sub>2</sub> PSA

A four-column H<sub>2</sub> PSA unit is designed such that a providing purge step is located between the two depressuring pressure equalisation (DPE) steps while the two pressurising pressure equalisation (PPE) steps take place in a row after the purge step as shown in Fig. 3. The step configuration was reconstructed referring to those in the literature (Cassidy 1980).

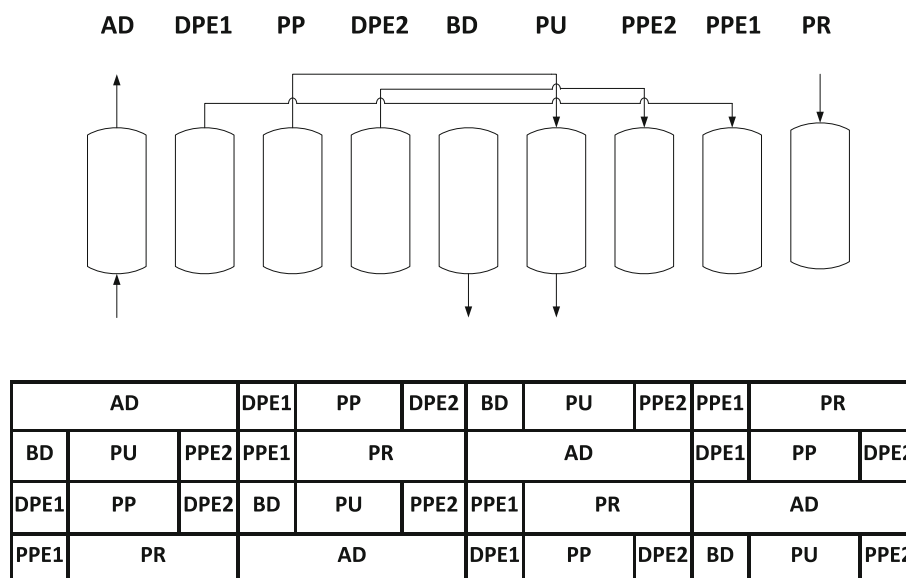
In the four-column H<sub>2</sub> PSA simulation, the total cycle time was fixed at 800 s with the adsorption step time equivalent to 1/4th of the cycle time as shown in Fig. 3. The purge flow is generated by reducing the column pressure starting from a pressure at the end of the first DPE step to a pressure that can be chosen at an operator's disposal. The equilibrated pressure at the start (or end) of the second DPE step (or its associated PPE step) is subject to how much purge flow is generated during the providing

purge step. Accordingly, the equilibrated pressure at the end (or start) of the first DPE step (or its associated PPE step) is also affected by the amount of purge flow. The step configuration where the providing purge step is located between the two DPE steps has a clear advantage over a cycle where the providing purge step follows the two DPE steps in that it can increase the purge flowrate to a greater extent since the providing purge step can start at a higher pressure. Therefore, this configuration is capable of controlling the product purity in a wider range without having to change the cycle time. It should be noted that the pressure recovery during the pressure equalisation in this four-column H<sub>2</sub> PSA would decrease with an increasing purge flowrate since the equilibrated pressure at the end of each pressure equalisation stage is affected by the amount of purge flow as shown in Fig. 4. By contrast the pressure recovery can be maintained at a constant level regardless of the change of purge flowrate in the configuration where the providing purge step is located after finishing all the DPE steps.

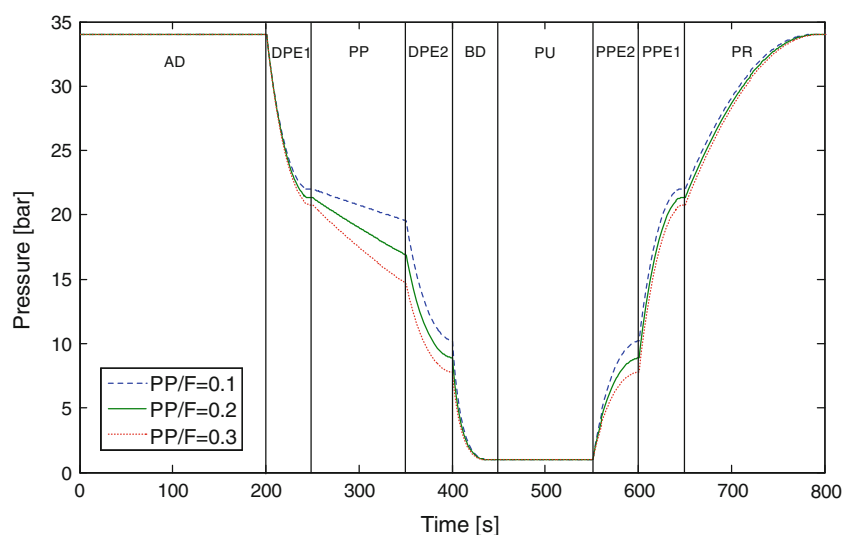
As shown in Fig. 4, the pressure profile of a column over a cycle is varied in response to the use of the different amounts of the purge flow investigated in this study. The actual flowrate of the purge gas flowing between two columns under the providing purge and purge steps respectively must decrease with the step time since the driving



**Fig. 3** Step configuration of a four-column PSA cycle (*AD* adsorption, *DPE* depressurising pressure equalisation, *PP* providing purge, *BD* blowdown, *PU* purge, *PPE* pressurising pressure equalisation, *PR* product pressurisation,  $t_{AD} = t_{cycle}/4$ ;  $t_{PR} = 3t_{cycle}/16$ ;  $t_{PP} = t_{PU} = t_{cycle}/8$ ;  $t_{BD} = t_{DPE} = t_{PPE} = t_{cycle}/16$ )



**Fig. 4** Pressure profiles at the product end of a column over a cycle at the cyclic steady state of the four-column  $H_2$  PSA unit: effect of the different amounts of purge flow



force diminishes with decreasing pressure difference between the columns. Therefore, an index of  $PP/F$  to quantify the varying purge flow as an average purge flow is introduced in this study. The  $PP/F$  denotes the ratio of an average purge flowrate being generated from one column during the providing purge step to a feed flowrate to one column for adsorption during one cycle. Note that the amount of the feed flowing to one column is not the same as the total amount of the feed flowing to a PSA system in case that more than one column share total feed flow. The different numbers of  $PP/F$  chosen at the three runs are shown in Fig. 4 and Table 3. As expected, the start and end pressures during the providing purge step becomes lower with an increase of the  $PP/F$ .

The targeted  $H_2$  purity of 99.99+ mol% is achieved in Run 2 where during the providing purge step the column

**Table 3** Performances of the four-column PSA system at different purge flow rates

Run	Adsorption time (s)	$H_2$ purity (%)	$H_2$ recovery (%)	$H_2$ productivity (mol $H_2$ /kg $_{ads}$ /day)
Run 1 ( $PP/F = 0.1$ )	200	99.976	75.09	168.06
Run 2 ( $PP/F = 0.2$ )	200	99.995	72.68	162.67
Run 3 ( $PP/F = 0.3$ )	200	99.999	70.56	157.93

pressure changes from 21.5 to 17 bar that is equivalent to a  $PP/F$  of 0.2. At this operating condition, the  $H_2$  recovery and productivity are 72.68 % and 162.67 mol $H_2$ /kg/day, respectively.

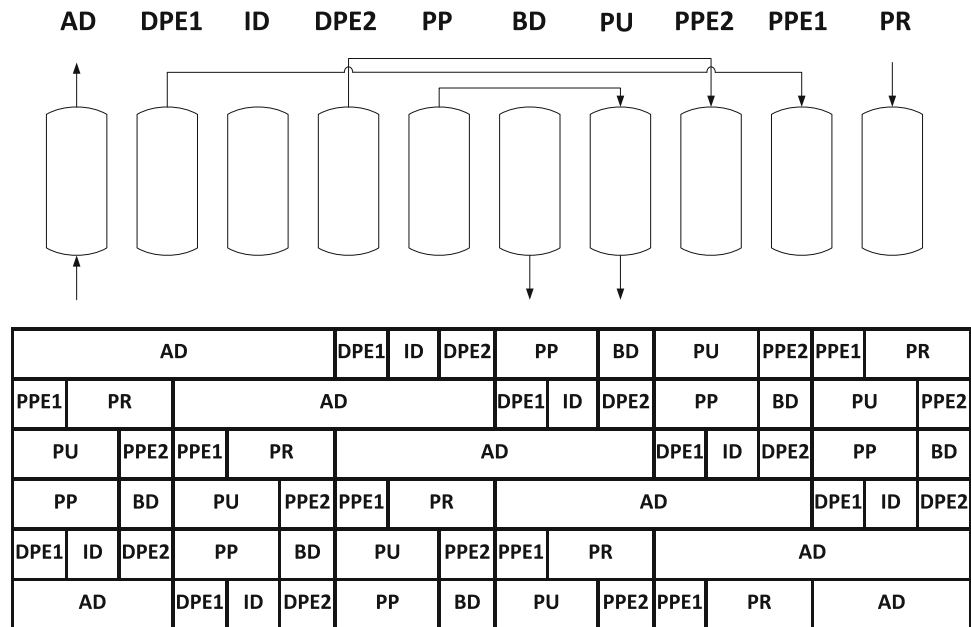
## 4.2 Six-column H<sub>2</sub> PSA

In the case of six-column H<sub>2</sub> PSA systems, two different step configurations were investigated. The first configuration (Fig. 5) features feeding the raw H<sub>2</sub> to two columns at the same time, that is to say, each of two columns receiving half the raw H<sub>2</sub> feed (Malek and Farooq 1997). Due to two columns being used for adsorption in a cycle, the first configuration cannot accommodate an additional pressure equalisation step but has the two-stage pressure equalisation that is the same as the above-mentioned four-column PSA system. Contrary to

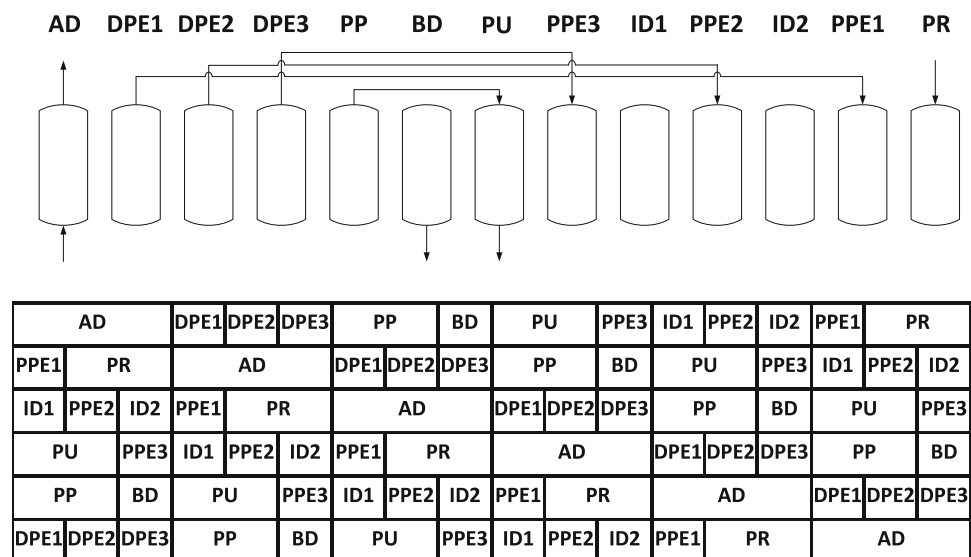
the four-column PSA system, a providing purge step is placed after the two pressure equalisation steps as shown in Fig. 5. It is anticipated that the alteration to the step configuration would be capable of improving the H<sub>2</sub> recovery since more pressure can be recovered during the pressure equalisation steps, that is to say, less consumption of pure hydrogen for product pressurisation and the reduced feed flowrate to one column for adsorption enables more efficient use of column due to less ingress of impurities into the product end.

In the second configuration (Fig. 6), however, only one column is taken up for high pressure adsorption in a cycle

**Fig. 5** Step configurations of a six-column PSA cycle with two-stage pressure equalisation (*AD* adsorption, *DPE* depressurising pressure equalisation, *ID* idle, *PP* providing purge, *BD* blowdown, *PU* purge, *PPE* pressurising pressure equalisation, *PR* pressurisation,  $t_{AD} = t_{cycle}/3$ ;  $t_{PP} = t_{PU} = t_{PR} = t_{cycle}/9$ ;  $t_{BD} = t_{DPE} = t_{PPE} = t_{ID} = t_{cycle}/18$ )

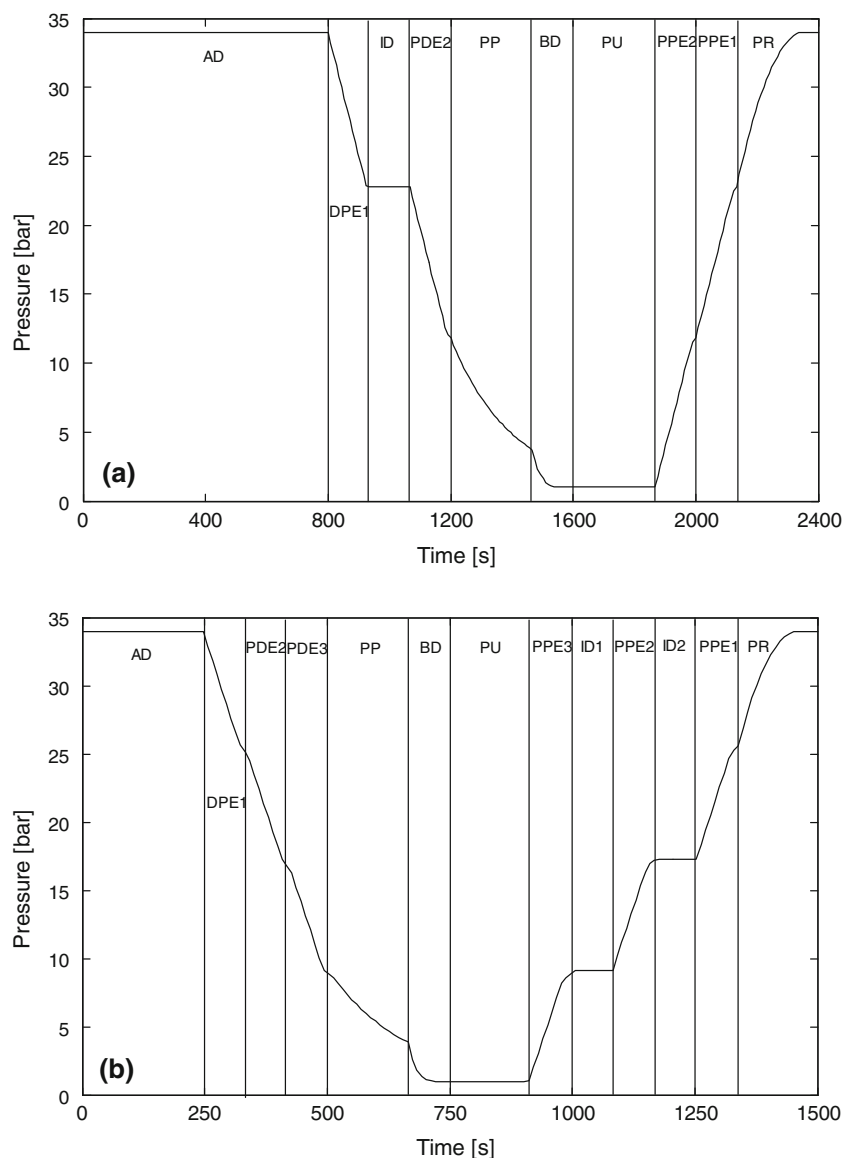


**Fig. 6** Step configurations of a six-column PSA cycle with three-stage pressure equalisations (*AD* adsorption, *DPE* depressurising pressure equalisation, *PP* providing purge, *BD* blowdown, *PU* purge, *ID*: idle, *PPE* pressurising pressure equalisation, *PR* pressurisation,  $t_{AD} = t_{cycle}/6$ ;  $t_{PP} = t_{PU} = t_{PR} = t_{cycle}/9$ ;  $t_{BD} = t_{DPE} = t_{PPE} = t_{ID} = t_{cycle}/18$ )





**Fig. 7** Pressure profiles at the product end of a column over a cycle at the cyclic steady state of six-column  $H_2$  PSA simulations at  $PP/F = 0.3$  with **a** two-stage pressure equalisation (Run 6) and **b** three-stage pressure equalisation (Run 10)



just as in the four-column  $H_2$  PSA. Therefore, it is possible to configure a PSA cycle with three-stage pressure equalisation (Xu 2002). It is generally expected that the more pressure equalisation stages a PSA cycle contains the higher hydrogen recovery can be obtained. This is because less hydrogen product is required during the product pressurisation step since the column can be pressurised to a higher pressure in advance during the PPE steps.

Figure 7 clearly exhibits the change of the pressure profile caused by adding one more pressure equalisation step to a PSA cycle. The first configuration having only two pressure equalisation steps (Fig. 7a) recovers less pressure during the pressure equalisation steps and consumes more hydrogen product during the product pressurisation step than the second configuration with three-stage pressure equalisation (Fig. 7b) does.

As observed in Table 4, the first and second configurations can achieve the targeted  $H_2$  purity (99.99+ mol%) at the cycle times of 2,400 and 1,500 s, respectively (Run 6 and 10). The adsorption time in Run 6 (800 s) is more than three times longer than that in Run 10 (250 s) even though the feed gas entering one column for adsorption is just halved in flowrate. This can be explained by two reasons. Firstly, the reduced feed flow to one adsorption column for adsorption prevents the ingress of impurities into the product end so it can allow a cycle to have a longer adsorption time. Secondly, the first configuration with only two-stage pressure equalisation has a better working capacity than the second configuration. This is because the column can be more thoroughly regenerated by a stream having more hydrogen and pressurised by more ultrapure hydrogen during the product pressurisation step, in other

**Table 4** Performance of six-column H<sub>2</sub> PSA simulations

Run	Adsorption time (s)	H <sub>2</sub> purity (%)	H <sub>2</sub> recovery (%)	H <sub>2</sub> productivity (mol <sub>H2</sub> /kg <sub>ads</sub> /day)
First configuration (two-stage pressure equalisation)				
Run 4	600	99.999	78.75	117.51
Run 5	700	99.996	81.98	122.33
Run 6	800	99.994	84.41	125.95
Run 7	900	99.975	86.29	128.75
Second configuration (three-stage pressure equalisation)				
Run 8	150	99.999	76.11	113.57
Run 9	200	99.997	82.47	123.05
Run 10	250	99.994	86.26	128.71
Run 11	300	99.969	88.79	132.48

words, the column is pressurised by gas streams coming from other columns during the pressure equalisation steps to a lesser extent. Therefore, it implies that the H<sub>2</sub> recovery would increase with more stages of pressure equalisation in a cycle but the working capacity of columns would deteriorate due to purging and pressurising the column with more impure gases.

It is noteworthy that the hydrogen recovery is enhanced around 12 % with the addition of two columns from four columns (Run 2) to six columns (Runs 6) only by changing the step configuration in spite of both having the same number of pressure equalisation steps. This change is not caused only by less hydrogen consumption during the product pressurisation step but also by the longer adsorption time.

At the operating condition of Run 10, the H<sub>2</sub> recovery increases further up to 86.26 % mainly due to enhanced pressure recovery taking place over the three-stage pressure equalisation. The stream leaving the column in the course of reducing the column pressure from 34 to 9 bar can be reused for pressurising other columns and significantly lower amount of hydrogen product is required for product pressurisation.

The H<sub>2</sub> productivities of both six-column H<sub>2</sub> PSA configurations are similar but lowered in comparison to that of the four-column H<sub>2</sub> PSA performance at the targeted H<sub>2</sub> purity. The change of the H<sub>2</sub> productivity can be explained with respect to the increasing number of columns (or increasing total amount of adsorbents being utilised) and the increasing H<sub>2</sub> recovery. The reduction of the H<sub>2</sub> productivity from four-column to six-column H<sub>2</sub> PSA is due to the increase of the H<sub>2</sub> recovery being less than the corresponding increase of the amount of adsorbent utilised.

#### 4.3 Polybed H<sub>2</sub> PSA (nine and twelve columns)

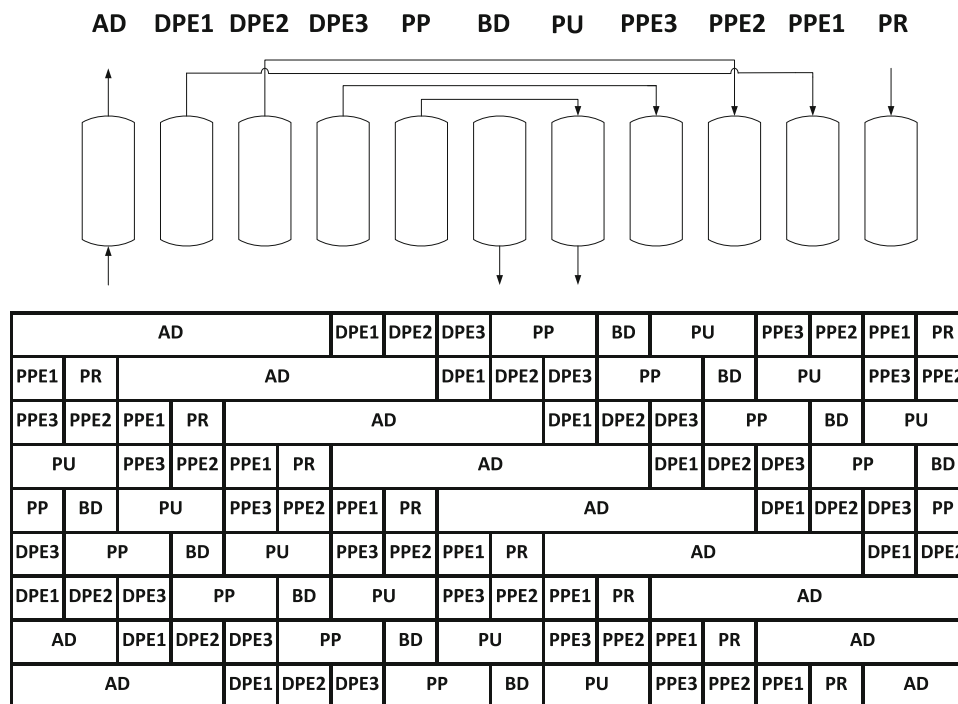
As mentioned above, as more columns are deployed a higher hydrogen recovery would be anticipated in a H<sub>2</sub>

PSA system. In this respect Polybed H<sub>2</sub> PSA processes containing seven to sixteen beds with at least three pressure equalisation steps and at least two columns receiving the feed gas for adsorption have been commercially operating for the purpose of H<sub>2</sub> purification (Yang 1987). In this study a nine-column eleven-step system is investigated following the step configuration found in the literature (Fuderer and Rudelstorfer 1976) as shown in Fig. 8. Figure 9 shows the pressure profile of the nine-column PSA system over a cycle at its cyclic steady state.

The nine-column eleven-step H<sub>2</sub> PSA system benefits from both reduced feed flowrate to one column and intensified pressure equalisation that each of the two six-column H<sub>2</sub> PSA systems has. The feed flowrate fed to one column for adsorption is reduced to one-third of the total feed flowrate since three out of nine columns always work for adsorption at the same time. The product pressurisation step starts at 26 bar and the providing purge step commences at 9 bar both of which are similar to those at the second configuration of six-column H<sub>2</sub> PSA system as shown in Figs. 7b and 9. This is because both PSA systems contain the same number of stages of pressure equalisation in their cycle.

Finally, a twelve-column thirteen-step H<sub>2</sub> PSA system was investigated in order to increase the H<sub>2</sub> recovery close to its maximum. The step configuration is presented in Fig. 10 that was originally shown in a patent (Xu et al. 2003). The step configuration features simultaneous adsorption at three columns, simultaneous providing purge and purge at two columns, and four-stage pressure equalisation. Thanks to one additional pressure equalisation step, the product pressurisation step starts at 27 bar and the providing purge step commences at 7.5 bar as shown in Fig. 11.

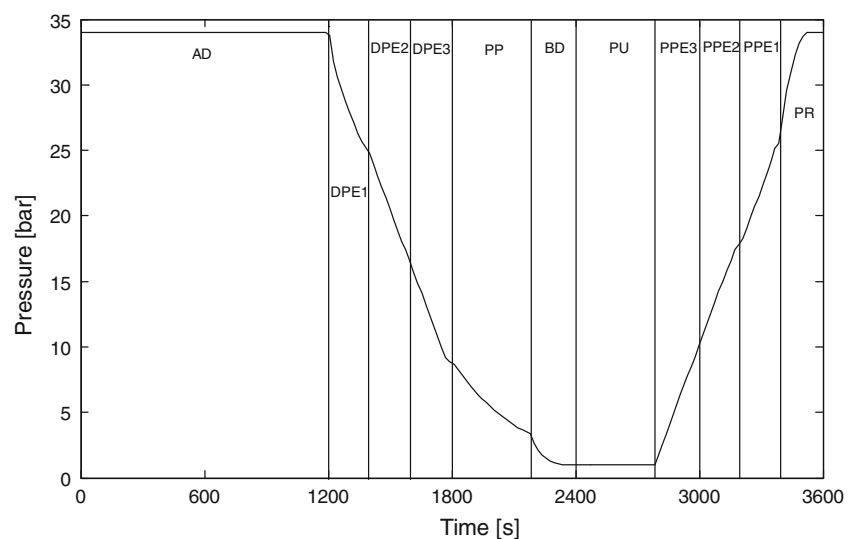
Table 5 lists the performance of the nine- and twelve-column H<sub>2</sub> PSA systems at their cyclic steady state. The nine-column H<sub>2</sub> PSA system can achieve the targeted H<sub>2</sub> purity at the adsorption step time of 1,200 s (Run 14). It should be noted that the adsorption step time of the twelve-column H<sub>2</sub> PSA to achieve the targeted H<sub>2</sub> purity (1,050 s at Run 18) is shorter than that of the nine-column H<sub>2</sub> PSA in spite of the same feed flowrate fed to one column, i.e. one-third of the total feed flowrate. This indicates that the column working capacity starts to deteriorate due to more incomplete regeneration by a purge flow having less hydrogen and by pressurising the column with more impure streams coming from other columns during the PPE steps instead of ultrapure hydrogen during the product pressurisation step. Nevertheless, the H<sub>2</sub> recovery still increases from 91.85 % at the nine-column H<sub>2</sub> PSA to 92.74 % at the twelve-column H<sub>2</sub> PSA. Since the improvement of the H<sub>2</sub> recovery is minimal, the H<sub>2</sub> productivity decreases significantly from 91.41 mol<sub>H2</sub>/kg<sub>ads</sub>/day at the nine-column H<sub>2</sub>



**Fig. 8** Step configurations of a nine-column PSA cycle (*AD* adsorption, *DPE* depressurising pressure equalisation, *PP* providing purge, *BD* blowdown, *PU* purge, *PPE* pressurising pressure equalisation, *PR*

pressurisation,  $t_{AD} = t_{cycle}/3$ ;  $t_{PP} = t_{PU} = t_{cycle}/9$ ;  $t_{BD} = t_{DPE} = t_{PPE} = t_{PR} = t_{cycle}/18$ )

**Fig. 9** Pressure profiles at the product end of a column over a cycle at the cyclic steady state of a nine-column  $H_2$  PSA at  $PP/F = 0.3$



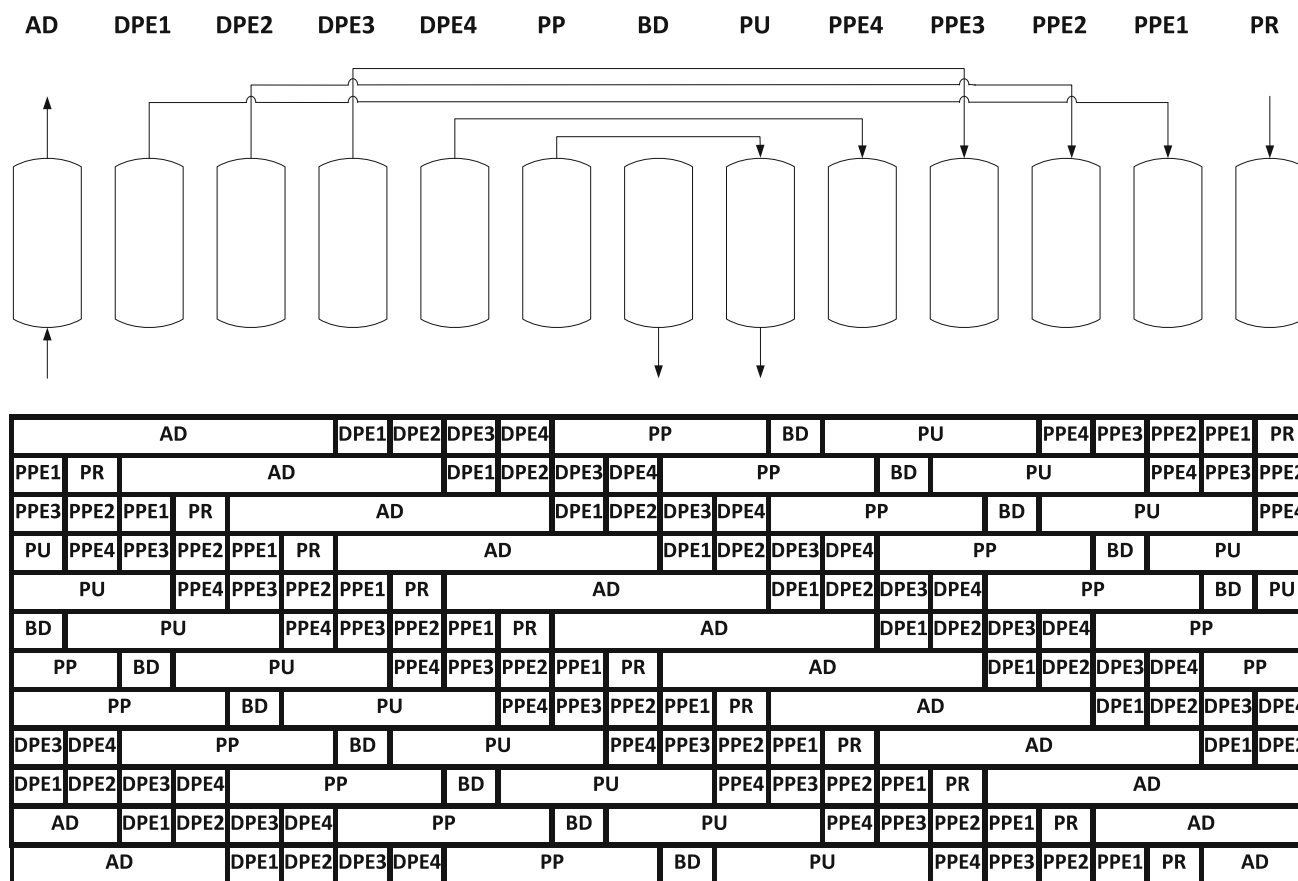
PSA to  $69.15 \text{ mol}_{H_2}/\text{kg}_{ads}/\text{day}$  at the twelve-column  $H_2$  PSA.

#### 4.4 Comparison among various PSA cycles

Up to now the  $H_2$  recovery and productivity are compared at the targeted  $H_2$  purity of around 99.99+ mol% among various  $H_2$  PSA cycles having different number of columns and different step configurations. Again the  $H_2$  productivity

is reduced with the increasing number of columns while the  $H_2$  recovery improves. All the simulation results are plotted on Fig. 12 indicating a clear trade-off between hydrogen purity and recovery.

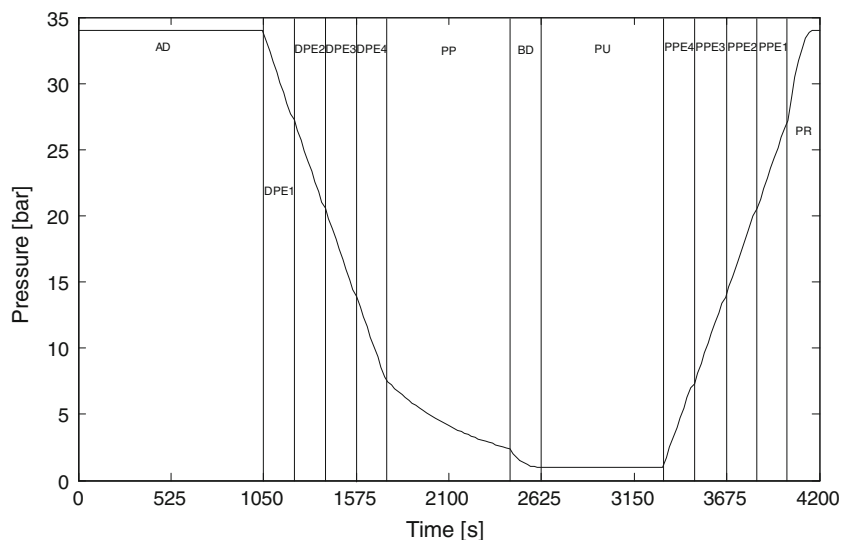
It is expected that more-than-twelve-column  $H_2$  PSA configuration may improve the  $H_2$  recovery further to more than 93 % but given the trend of improving  $H_2$  recovery with the number of columns a further improvement of  $H_2$  recovery would be very limited. In particular, more than



**Fig. 10** Step configurations of a twelve-column PSA cycle (*AD* adsorption, *DPE* depressurising pressure equalisation, *PP* providing purge, *BD* blowdown, *PU* purge, *PPE* pressurising pressure

equalisation, *PR* pressurisation,  $t_{AD} = t_{cycle}/4$ ;  $t_{PP} = t_{PU} = t_{cycle}/6$ ;  $t_{BD} = t_{DPE} = t_{PPE} = t_{PR} = t_{cycle}/24$ )

**Fig. 11** Pressure profiles at the product end of a column over a cycle at the cyclic steady state of a twelve-column  $H_2$  PSA at  $PP/F = 0.3$



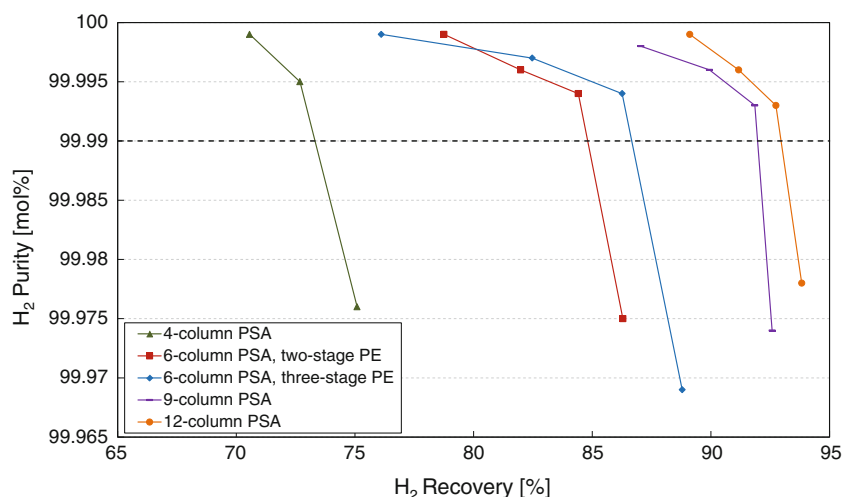
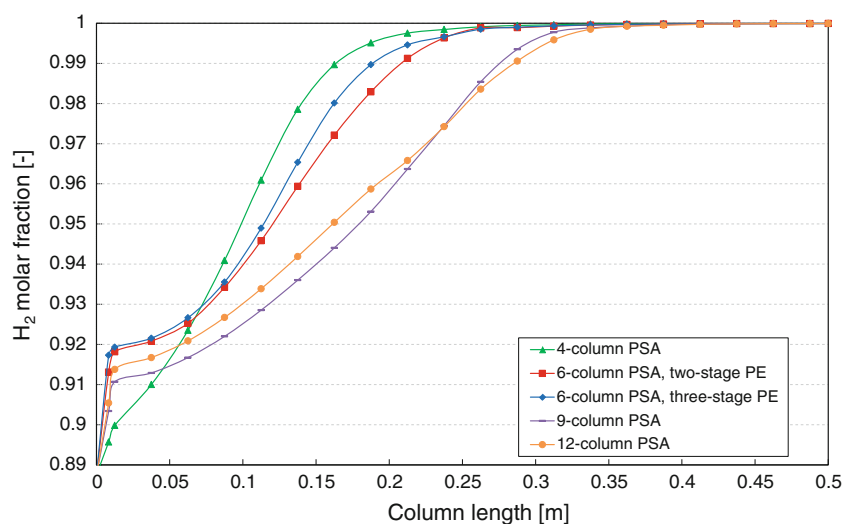
five stage pressure equalisation steps may not be necessary since the column pressure at the end of the fourth DPE (or PPE) step in the twelve-column  $H_2$  PSA is very close to

that at the end of the third DPE (or PPE) step in the nine-column  $H_2$  PSA systems. Therefore, altering a PSA cycle to have more than five pressure equalisation steps cannot

**Table 5** Performance of nine-column and twelve-column PSA simulations

Run	Adsorption time (s)	H <sub>2</sub> purity (%)	H <sub>2</sub> recovery (%)	H <sub>2</sub> productivity (mol <sub>H<sub>2</sub></sub> /kg <sub>ads</sub> /day)
Nine-column H <sub>2</sub> PSA				
Run 12	800	99.998	87.05	86.64
Run 13	1,000	99.996	89.94	89.51
Run 14	1,200	99.993	91.85	91.41
Run 15	1,300	99.974	92.58	92.14
Twelve-column H <sub>2</sub> PSA				
Run 16	750	99.999	89.11	66.52
Run 17	900	99.996	91.17	68.06
Run 18	1,050	99.993	92.74	69.15
Run 19	1,200	99.978	93.83	70.04

recover a notable pressure nor save the amount of ultrapure hydrogen consumed during the product pressurisation step significantly. In addition, it is likely that the working

**Fig. 12** Comparison of hydrogen purity and recovery at various H<sub>2</sub> PSA systems with the different number of columns and different step configurations**Fig. 13** Hydrogen molar fraction profiles along the column at the end of the adsorption step in various PSA cycles at around 99.99 % H<sub>2</sub> purity

capacity of the column would be badly affected by incomplete regeneration with purge flow having less hydrogen and pressurisation of the column by more impure gas streams than the pure product streams.

Figure 13 shows the hydrogen mole fraction profile along the column at the end of the adsorption step at the cyclic steady state of all the PSA simulation investigated in this study. It clearly shows that with the reduction of the feed flow to one-column for adsorption from four-column to nine-column through six-column with two-stage pressure equalisation the PSA system allows a cycle to have longer adsorption step time so the H<sub>2</sub> mass transfer zone (MTZ) can progress more to the product end at the end of adsorption step. This results in less H<sub>2</sub> remaining at the end of the adsorption step leading to a higher H<sub>2</sub> recovery. The figure also shows that the twelve-column PSA has a broader H<sub>2</sub> MTZ than the nine-column PSA does due to worse regeneration of the column during the purge step and pressurisation with more impure stream while the column is pressurised.

## 5 Conclusions

A novel H<sub>2</sub> PSA system to produce ultrapure hydrogen from a raw H<sub>2</sub> gas generated in an advanced IGCC process has been proposed in this study. The advanced IGCC plant where CO<sub>2</sub> is intrinsically captured by a pre-combustion capture unit is capable of cogenerating both power and ultrapure hydrogen more economically. The advanced IGCC plant can be used in oil refineries having difficulty in sourcing ultrapure hydrogen that is required to operate hydrotreaters and hydrocrackers and intending to reduce carbon emission from their hydrogen and power plants.

To know the maximum H<sub>2</sub> recovery that a H<sub>2</sub> PSA can produce from the raw H<sub>2</sub> gas is very important in evaluating the performance of the advanced IGCC plant for cogenerating power and ultrapure hydrogen. This is because the flowrate of PSA tail gas, to be determined by the H<sub>2</sub> recovery, should be compressed up to 34 bar from the purge pressure to get the PSA tail gas fed to the gas turbine along with the fuel gas. Therefore, it is essential to design a H<sub>2</sub> PSA such that its H<sub>2</sub> recovery can be maximised in order to minimise the power consumption relating to tail gas compression.

H<sub>2</sub> PSA in commercial SMR hydrogen plants is capable of achieving around 89 % H<sub>2</sub> recovery at the 99.99+ % H<sub>2</sub> purity. Compared to the raw H<sub>2</sub> gas in the SMR hydrogen plant, the raw H<sub>2</sub> gas fed to the H<sub>2</sub> PSA in the advanced IGCC plant has a gas composition of higher hydrogen and lower impurities and the higher total pressure at which conditions the H<sub>2</sub> PSA is expected to perform better than the H<sub>2</sub> PSA in a SMR H<sub>2</sub> plant. As expected, the Polybed H<sub>2</sub> PSA having twelve columns achieves 93 % H<sub>2</sub> recovery at 99.99+ mol% H<sub>2</sub> purity.

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